

# Practical Macroscopic Evaluation and Comparison of Railway Timetables

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# Comparing and Preferring Timetables

## Belgian Infrastructure Management Company: Infrabel:

Compare 2 Timetables in terms of Expected Passenger Travel Time  
(includes: ride, dwell, transfer time and primary and secondary delays)

## Note:

Including primary and secondary delays  
⇒ evaluate efficiency & robustness

## Specifics:

One Busy Day, Morning Peak Hour

# Result of Reflowing: Disc Area = Daily Flow

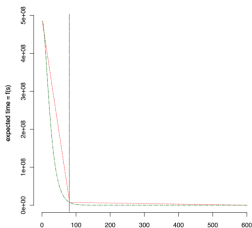


# In-Time and Over-Time

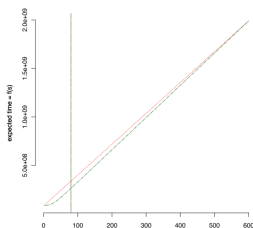
**Table 1:** In-Time and Over-Time Integrals when adding supplement  $D_0$

	In-Time	Over-Time
probability inc./dec. in $D_0$	$\int_0^{D_0} p_a(x) dx$ inc.	$\int_{D_0}^{D_1} p_a(x) dx$ dec.
expected time inc./dec. in $D_0$	$\int_0^{D_0} p_a(x) D_0 dx$ inc.	$\int_{D_0}^{D_1} p_a(x) D_1 dx$ dec.
departing = ride' + dwell' + source		✓
through = ride + dwell	✓	
changing = ride + transfer	✓	✓
arriving = ride + sink	✓	

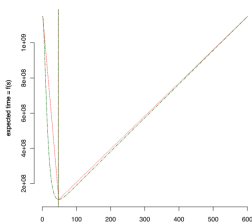
# Cost curves of 4 Passenger Categories



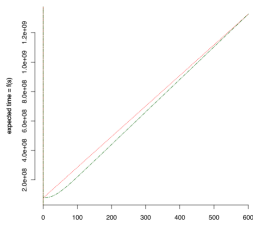
(a) departing =  $\text{ride}' + \text{dwell}' + \text{source}$



(b) through =  $\text{ride} + \text{dwell}$

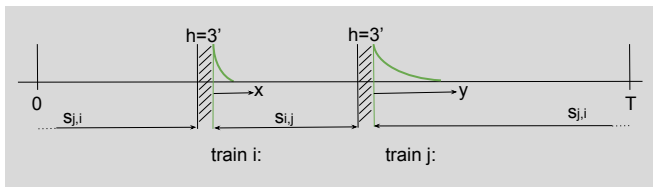


(c) changing =  $\text{ride} + \text{transfer}$

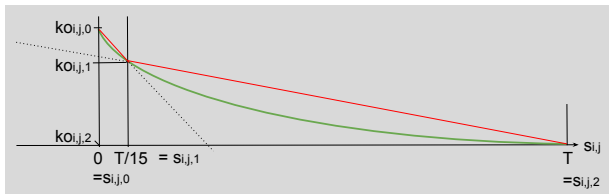


(d) arriving =  $\text{ride} + \text{sink}$

# All Knock-On Costs for $N(N - 1)$ Trains on Same Resource: Formula



$$\forall R : pKO_R = \sum_{\substack{i,j \in I_R \\ i \neq j}} f_j \cdot \frac{a_j e^{-a_i S_{i,j}}}{a_i (a_i + a_j)}. \quad (1)$$



## Results for Hard Constraints: Realisability?

**Table 2:** Realisability. Reduction of the number and size of minimum runtime violations from timetable T1  $\rightarrow$  T2.

timetable	distribution: # actions with a violation per size of violation in seconds										
	6s	12s	18s	24s	30s	36s	42s	48s	56s	60s	66s
T1	320	219	126	93	24	27	3	6	1	3	1
T2	277	155	84	37	11	2	2	2			

**Table 3:** Realisability. Reduction of total and average violation from timetable T1  $\rightarrow$  T2.

timetable	weighted sum (s)	tot.#	avg. (s)
T1	11454	823	13.9
T2	6504	570	11.4

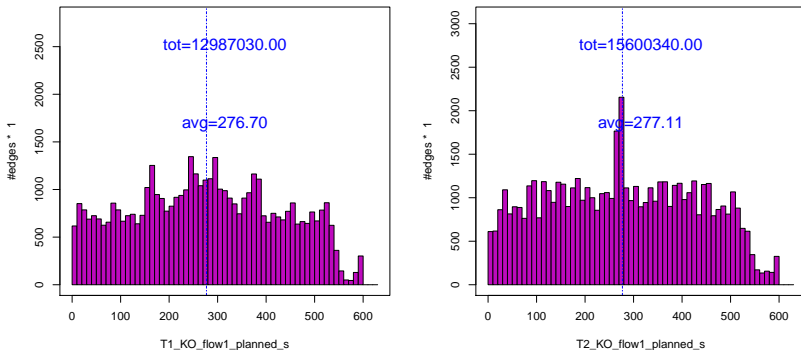


# Results for Hard Constraints: Minimum Run Time Violations.

From run time check table:

- Both T1 and T2 have minimum run time violations.
- So are not realisable.
- T2 has fewer and smaller run time violations than T1.

# Results for Hard Constraints: Headway Conflicts?



**Figure 1:** Planned headway supplements, in T1 and T2 of:  $T - 3' \leq s < T$ , are problematic.

## Results for Hard Constraints: Headway Conflicts.

From headway histograms:

- Both T1 and T2 have minimum headway time violations.
- So are not feasible = not conflict-less.

# Results in the Planned Train Time Domain

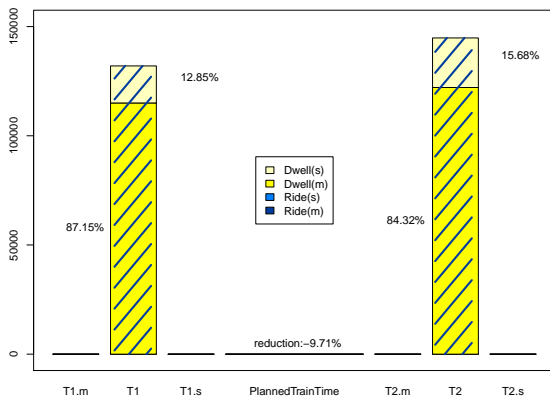


Figure 2: Increase of 9.71% of total planned train time from T1 to T2. All time units are in 6 second multiples.

## Results in the Planned Train Time Domain

Bargraphs show:  $T1 \rightarrow T2$

- more planned train minimum ride + dwell time:
  - due to some extra trains in T2 compared to T1,
  - effectiveness for passenger service of this is to be judged in expected passenger time domain.
- (relatively) more planned train ride + dwell supplement time:
  - efficiency versus robustness of this is to be judged in expected passenger time domain.

# Results in the Expected Passenger Time Domain

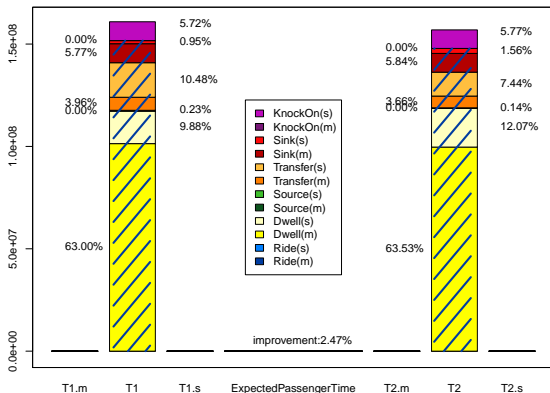


Figure 3: Reduction of 2.47% of total expected passenger time from T1 to T2. All time units are in 6 second multiples.

## Results in the Expected Passenger Time Domain

Bargraphs show: T1  $\rightarrow$  T2

- + less (expected) minimum ride + dwell time due to:
  - faster trains and/or
  - more effective direct connections (for big passenger OD pairs) (different line planning)
- - more expected ride + dwell supplement time  $\rightarrow$  less efficient
- = similar expected knock-on delay  $\rightarrow$  similar robustness
- + significantly reduced expected transfer time due to:
  - more effective transfers (for big passenger OD pairs)
- + overall reduction of 2.47% in expected passenger time
- + average probability of missing a transfer is reduced from 14.41% for T1 to 5.51% for T2.

# International Comparison

Table 4: Current Quality Levels of some European Railway Timetables

Level	realisable no min. run/dwell violations	conflictless no min. headway violations	robust	resilient	Country
	feasible				
	deterministic		stochastic		
0					FR, IT, BE, DK
1	v				NL, UK
2	v	v			DE
3	v	v	v		CH, SE, BE', DK'
4	v	v	v	v	

- All text in black above is due to [Goverde and Hansen(2013)]
- [Sels et al.(2015a)Sels, Cattrysse, and Vansteenwegen]
- [Sels et al.(2015b)Sels, Dewilde, Cattrysse, and Vansteenwegen]
- [Sels et al.(2015c)Sels, Dewilde, Cattrysse, and Vansteenwegen]
- \*Note: Our optimized timetables: BE',DK' are stable, *have no 'macroscopic conflicts'* and are robust.



# Conclusions





- practical method to evaluate and compare timetables
- objective = evaluation function = minimal expected passenger time
- showed T1  $\rightarrow$  T2 reduction of 2.47% in exp. passenger. time
- evaluation reports on hard constraints, deterministic
  - realisability (ride & dwell & transfers)
  - conflict freeness (headways)
  - stability (cycles)
- evaluation reports on soft constraints, stochastic
  - efficiency
  - robustness
  - (resilience)

# Future Work

- evaluate over only real transfers ← data?
- vary parameter 'a' value: 1% .. 5%
- add parameter 'r'
  - r% of passengers benefit from temporal spreading of trains
- parameter 'r' value: 0% .. 100%

# Questions

- Your questions?
  - here and now, or ...
  - [sels.peter@gmail.com](mailto:sels.peter@gmail.com)
  - [www.LogicallyYours.com/research/](http://www.LogicallyYours.com/research/)

-  Goverde, R., Hansen, I., 2013. Performance indicators for railway timetables. Proceedings of IEEE International Conference on Intelligent Rail Transportation: ICIRT2013, August 30-September 1, 2013, Beijing, China., 301–306.
-  Sels, P., Cattrysse, D., Vansteenwegen, P., Jul. 2015a. Practical Macroscopic Evaluation and Comparison of Railway Timetables. Proceedings of the 18th Euro Working Group on transportation (EWGT2015), 14-16 July 2015, Delft, The Netherlands. URL <http://4c4u.com/ED2015.pdf>.
-  Sels, P., Dewilde, T., Cattrysse, D., Vansteenwegen, P., 2015b. Reducing the Passenger Travel Time in Practice by the Automated Construction of a Robust Railway Timetable. submitted to Transportation Research Part B URL <http://4c4u.com/TRB2015.pdf>.
-  Sels, P., Dewilde, T., Cattrysse, D., Vansteenwegen, P., Jul. 2015c. Towards a Better Train Timetable for Denmark, Reducing Total Expected Passenger Time. Proceedings of the 13th Conference on Advanced Systems in Public Transport (CASPT2015), 19-23 July 2015, Rotterdam, The Netherlands. URL <http://4c4u.com/CR2015.pdf>.